



Final Presentation

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Commonwealth Fusion Systems



Overview

- Problem

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- Project Goal: Implement a solder model in Ansys

- ☒ Create a plastic flow equation based on the experimental data of 60Sn40Pb or 63Sn37Pb solder.
- ☒ Create an UPF usermat.F file containing the equation.

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1. Gather experiment data:

σ_y and E of Sn₆₀Pb₄₀ at 4K and 77K



Table 2 Mechanical properties of lead/tin solders

% Sn	Temperature (K)	σ_u (MPa)	σ_y (MPa)	Elongation %
100				
60				
50				
40				
0				
100				
60				
50				
40				
0				

%Sn	Temp [K]	Young's Modulus (at 0.2% strain) [GPa]

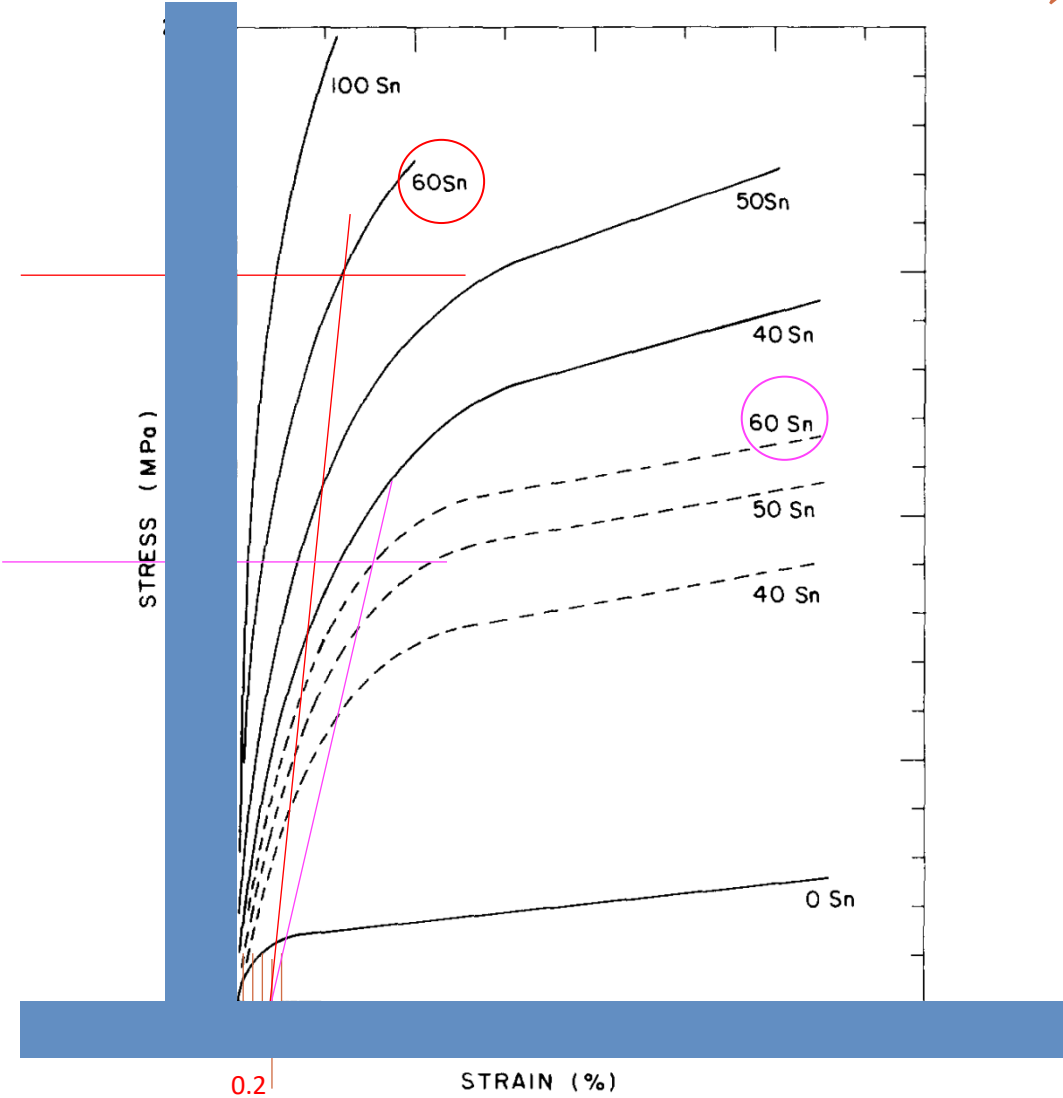


Figure 3 Stress-strain behaviour of various solders at 77 and 4.2 K.
—, 4.2 K; ----, 77 K

1. Gather experiment data:

E of $\text{Sn}_{63}\text{Pb}_{37}$ at 233K \rightarrow 398K

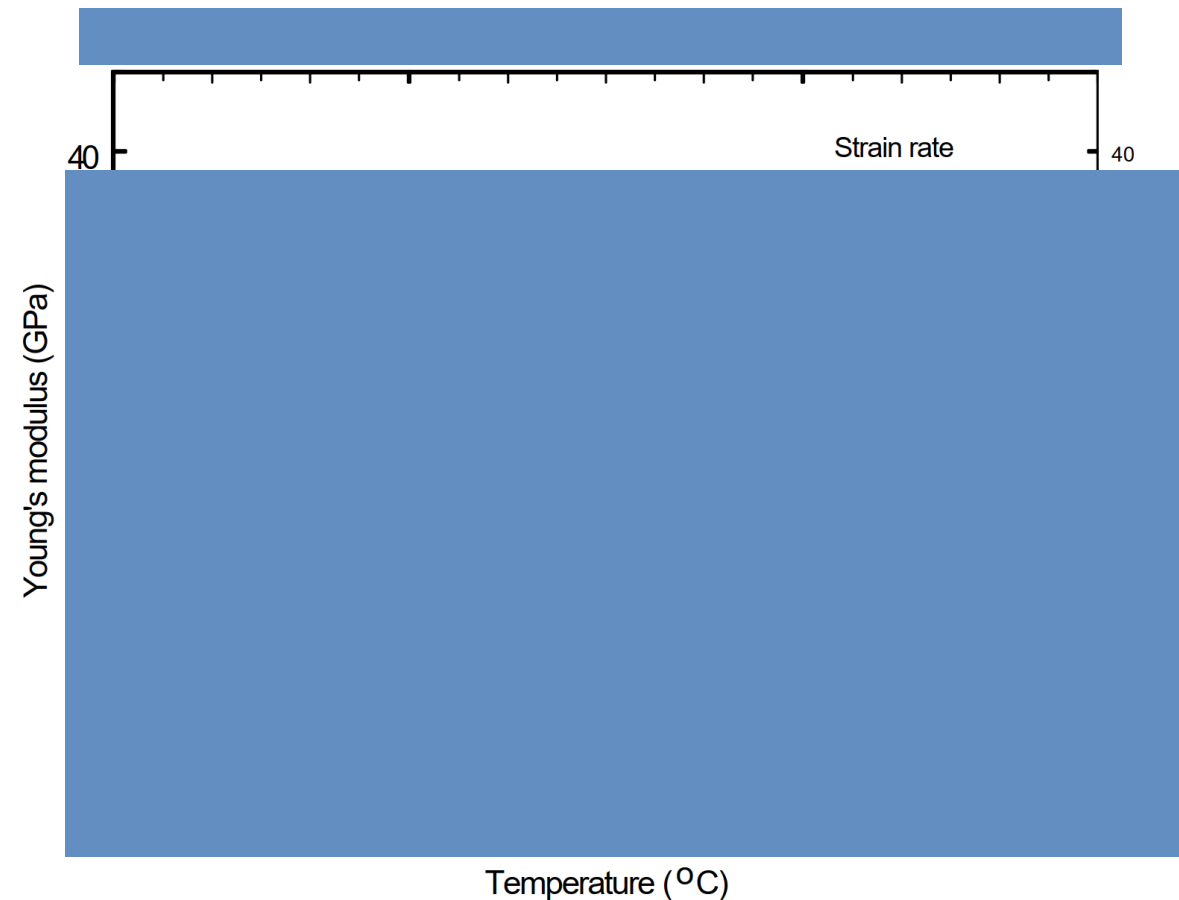


Fig. 3 Effect of temperature on Young's modulus

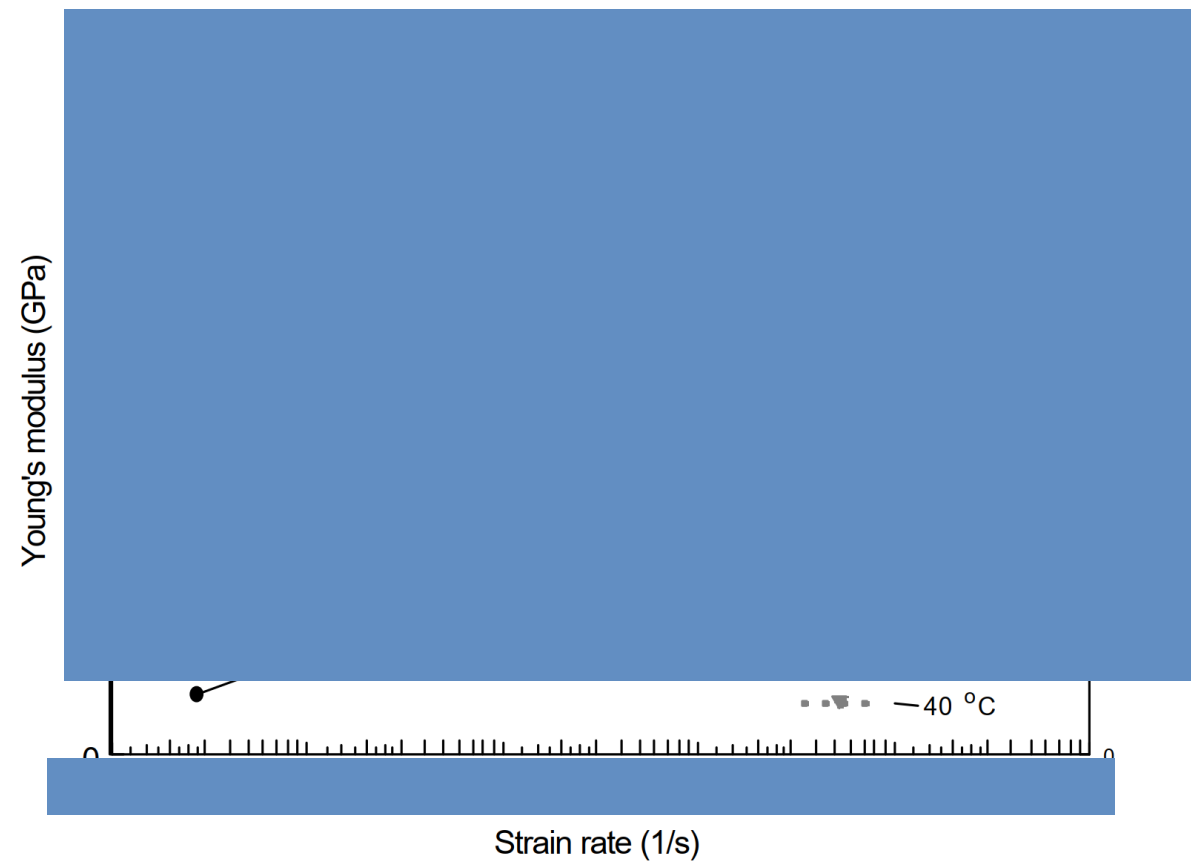


Fig. 4 Effect of strain rate on Young's modulus

1. Gather experiment data:

σ_y of Sn₆₃Pb₃₇ at 233K → 398K

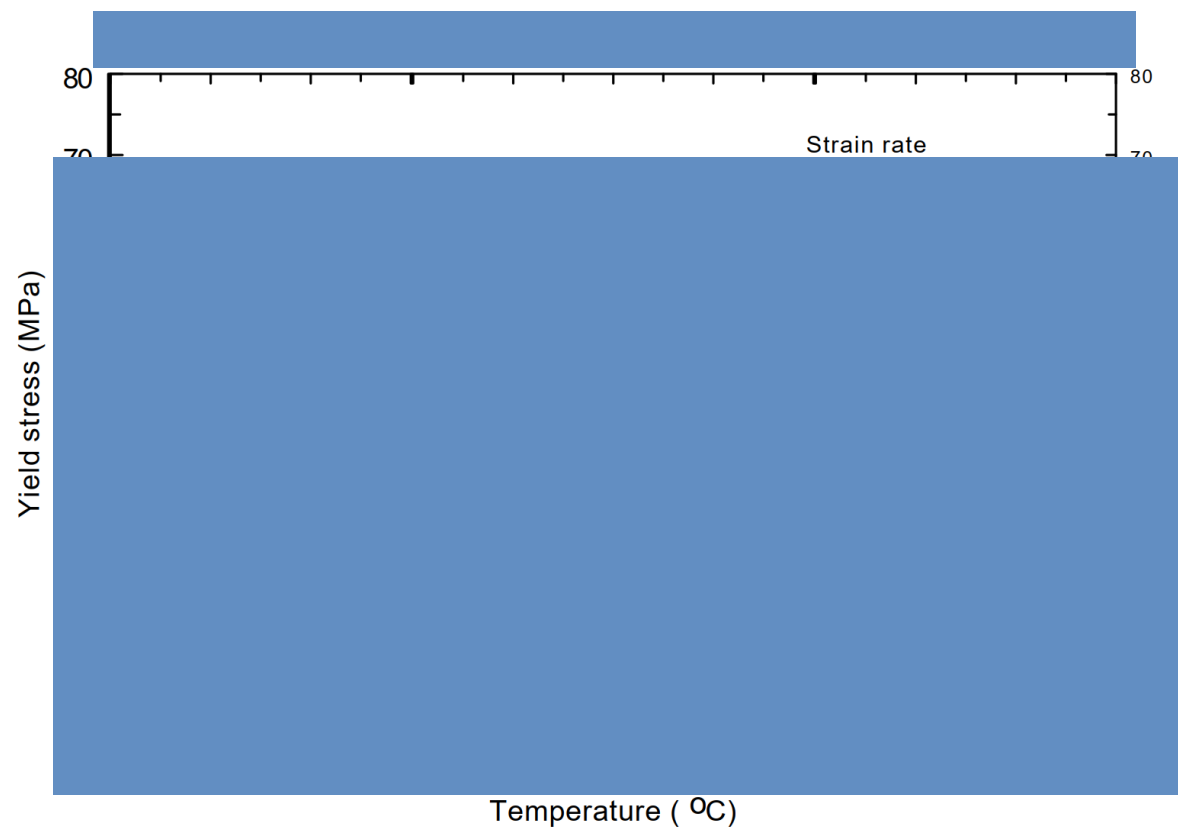


Fig. 5 Effect of temperature on yield stress

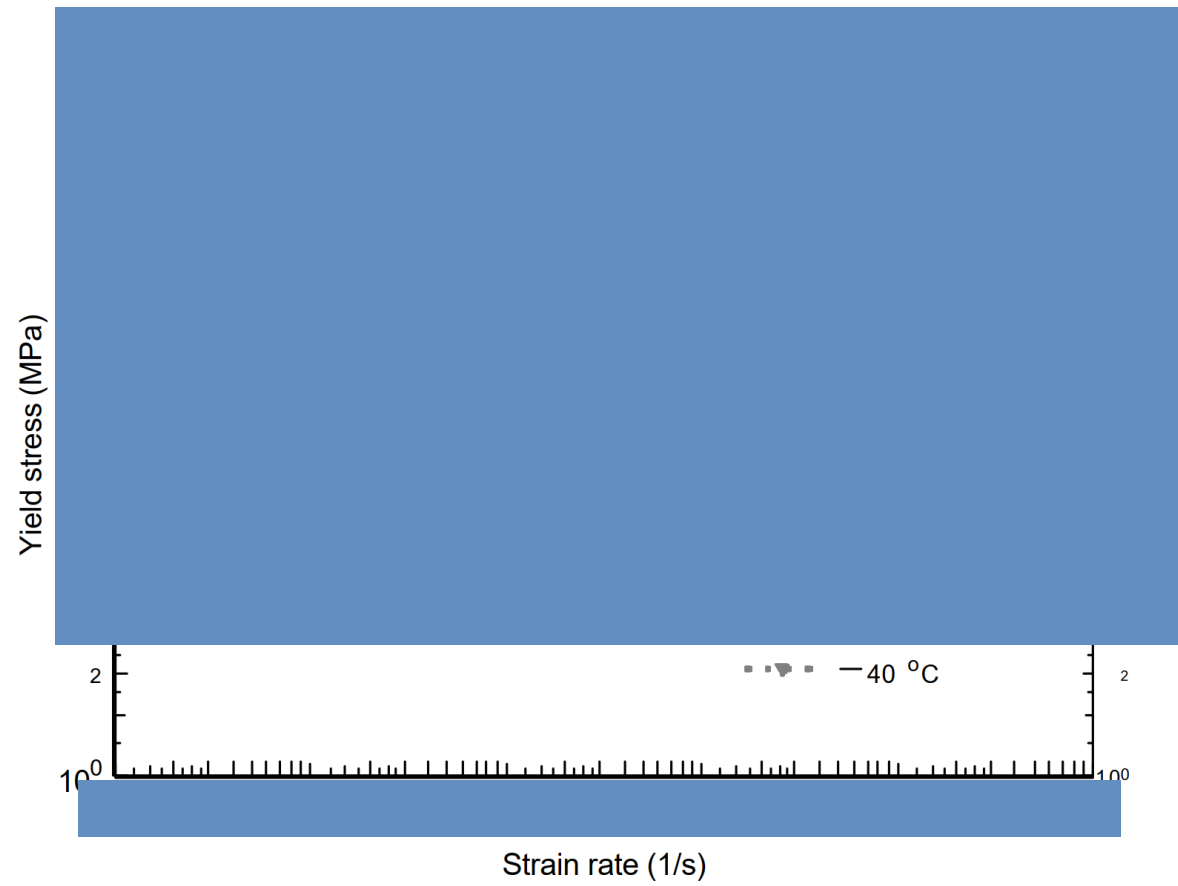


Fig. 6 Effect of strain rate on yield stress



1. Gather experiment data:

σ_y and E of Sn₆₀Pb₄₀ / Sn₆₃Pb₃₇ at 4K → 398K

Chosen for general material properties in Ansys

T [K]	$\dot{\epsilon} = 2.78\text{E-}5$ [1/s]		$\dot{\epsilon} = 2.78\text{E-}4$ [1/s]		$\dot{\epsilon} = 2.78\text{E-}3$ [1/s]		$\dot{\epsilon} = 2.78\text{E-}2$ [1/s]		$\dot{\epsilon} = 2.78\text{E-}1$ [1/s]		Poisson's ratio
	E [GPa]	σ_Y [MPa] at $\epsilon = 0.2\%$	E [GPa]	σ_Y [MPa] at $\epsilon = 0.2\%$	E [GPa]	σ_Y [MPa] at $\epsilon = 0.2\%$	E [GPa]	σ_Y [MPa] at $\epsilon = 0.2\%$	E [GPa]	σ_Y [MPa] at $\epsilon = 0.2\%$	



2. Re-create experiment data on plot via explicit integration method

- Loading conditions

- Max true strain: $\varepsilon_{T_{max}}$ \rightarrow Max engineering strain: $\varepsilon_{Eng_{max}}$
- Strain rate: $\dot{\varepsilon}$

$$\varepsilon_{T_{max}} = \ln(1 + \varepsilon_{Eng_{max}}) \quad (1)$$

$$\varepsilon_{n+1} = \varepsilon_n + \frac{\varepsilon_{Eng_{max}}}{N} \quad (2)$$

$$\varepsilon_{T_{n+1}} = \ln(1 + \varepsilon_{n+1}) \quad (3)$$

- Material properties

- Young's Modulus: E
- Initial deformation resistance: s_0
- Initial plastic strain rate: $\dot{\varepsilon}_0$
- Dimensionless constant: m, r
- Saturation value of deformation resistance: s_{sat}
- Hardening/softening constant: h_0

Calibrate

$$dt = \frac{\varepsilon_{T_{n+1}} - \varepsilon_{T_n}}{\dot{\varepsilon}} \quad (4)$$

$$t_{n+1} = t_n + dt \quad (5)$$

$$\dot{\varepsilon}_{p_{n+1}} = \dot{\varepsilon}_0 \left(\frac{|\sigma_n|}{s_n} \right)^{1/m} \quad (6)$$

$$\varepsilon_{p_{n+1}} = \varepsilon_{p_n} + \dot{\varepsilon}_{p_{n+1}} dt \cdot \text{sign}(\sigma_n) \quad (7)$$

$$\dot{s}_{n+1} = h_0 \left(1 - \frac{s_n}{s_{sat}} \right)^r \dot{\varepsilon}_{p_{n+1}} \quad (8)$$

$$s_{n+1} = s_n + \dot{s}_{n+1} dt \quad (9)$$

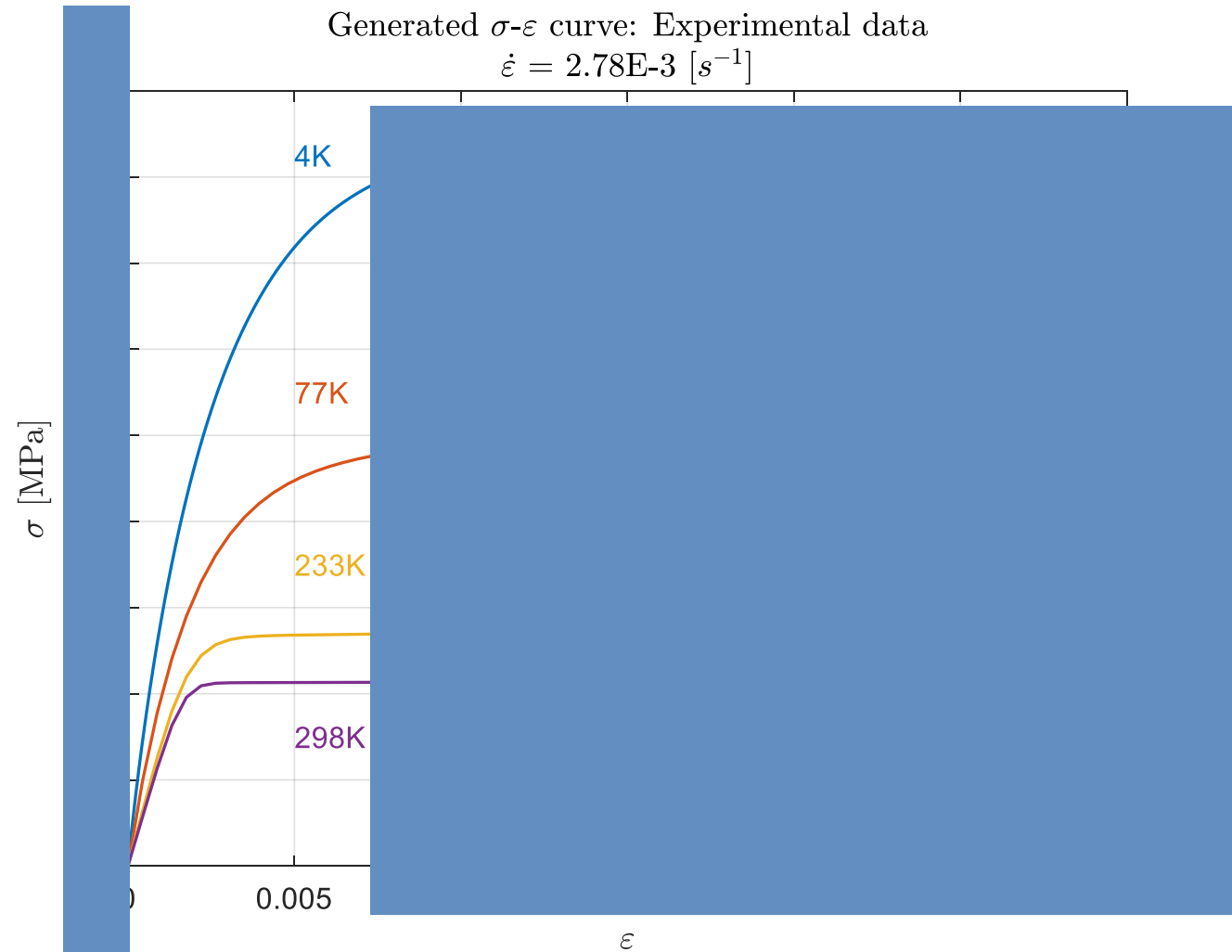
$$\varepsilon_{e_{n+1}} = \varepsilon_{T_{n+1}} - \varepsilon_{p_{n+1}} \quad (10)$$

$$\sigma_{n+1} = E \cdot \varepsilon_{e_{n+1}} \quad (11)$$

- Output

- Plastic strain rate: $\dot{\varepsilon}_p$
- Deformation resistance: s

2. Re-create experiment data on plot via explicit integration method





3. Create a temperature-dependent flow equation

- Initially, Anand's model is chosen: [Chen et al \(2017\) \[3\]](#)
 - No yield or loading conditions required.
 - The isotropic deformation resistance to plastic flow, s , is required
 - emphasizes T and $\dot{\epsilon}_p$ sensitivity + strain hardening + ...
 - Applicable to a wide range of temperature (i.e, 233K → 373K)
 - Is built-in in Ansys Engineering Data Toolbox.
 - However, the Arrhenius function $A \cdot e^{\frac{-Q}{kT}}$ is too steep for cryogenic temperature at 4K and 77K.

$$\dot{\epsilon}_p = \underbrace{A \cdot e^{\frac{-Q}{kT}}}_{\text{Arrhenius function}} \cdot \sinh\left(\frac{\xi \sigma}{s}\right)^{1/m}$$



3. Create a temperature-dependent flow equation

- Busso's model is chosen: [Chen et al \(2017\) \[3\]](#)
 - Emphasizes σ dependent activation energy F_0 and Bauschinger effect.
 - Suggests the dependence of T and $\dot{\epsilon}_p$ on shear stress.
 - However, the simplified version does not capture smooth elastic-plastic transition and isotropic hardening effect.

$$\sigma = \sigma_0 A \left\{ 1 - \left[\frac{\theta}{\frac{F_0}{R} \cdot \frac{1}{\ln(\dot{\epsilon}_0 / \dot{\epsilon}_p)}} \right]^{1/q} \right\}^{1/p}$$

$$\dot{\epsilon}_p = \frac{\dot{\epsilon}_0}{\exp \left\{ \frac{F_0}{\theta \cdot R} \left[1 - \left(\frac{\sigma}{\sigma_0 \cdot A} \right)^p \right]^q \right\}}$$



3. Create a temperature-dependent flow equation

- Fixed inputs
 - Temperature: θ
 - Gas constant: R
 - Yield stress at 0K: σ_0
 - Stress (from experiment data): σ
 - Plastic strain rate (from explicit integration, representing experiment data): $\dot{\epsilon}_p$

- Least-squared Optimization solutions

- Free activation energy: F_0
 - Shear Modulus ratio: A
 - Initial strain rate: $\dot{\epsilon}_0$
 - Material constants: p, q
- } Suggest initial values

$$\sigma = \sigma_0 A \left\{ 1 - \left[\frac{\theta}{\frac{F_0}{R} \cdot \frac{1}{\ln(\dot{\epsilon}_0 / \dot{\epsilon}_p)}} \right]^{1/q} \right\}^{1/p}$$

`diffexpr = sum(($\sigma_{calculated}$ - $\sigma_{experimental}$) .^2);`

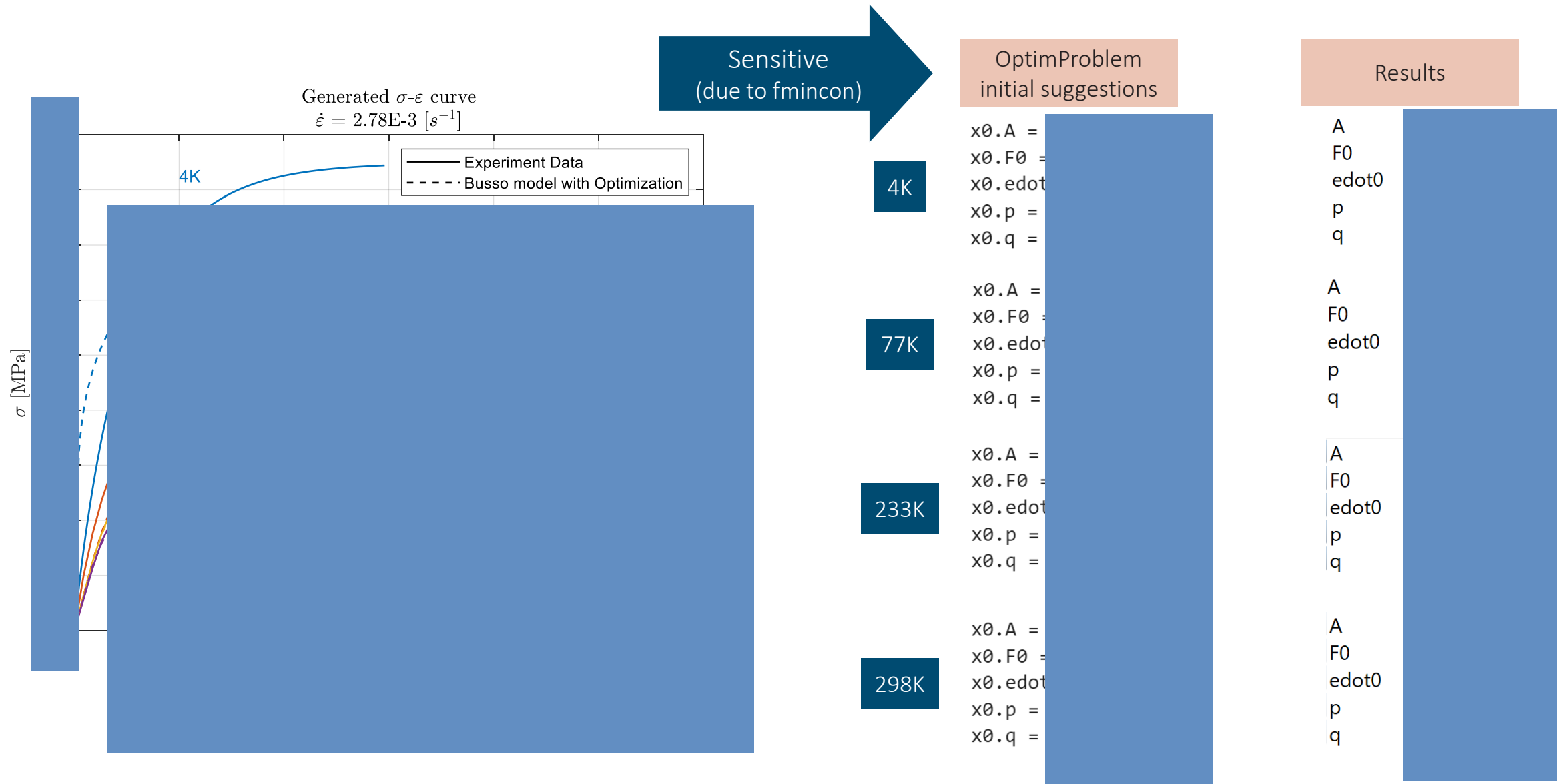
`ssqprob = optimproblem('Objective',diffexpr);`

`opts =
optimoptions('fmincon','MaxFunctionEvaluations',
30000,'Algorithm','sqp');`

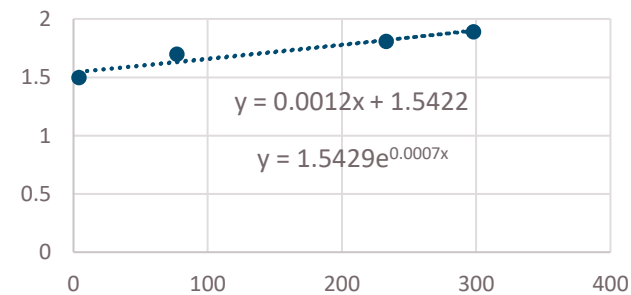
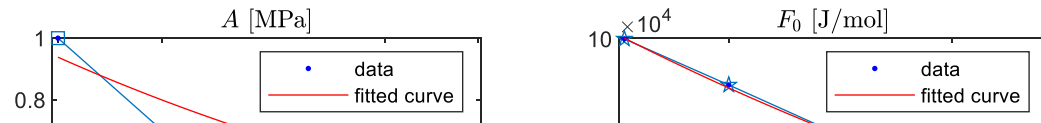
`[sol1,fval,exitflag,output] =
solve(ssqprob,x0,Options=opts);`

`resp1 = evaluate(diffun,sol1);`

3. Create a temperature-dependent flow equation



3. Create a temperature-dependent flow equation



Fitted equations generated by Excel is 'better' by MATLAB

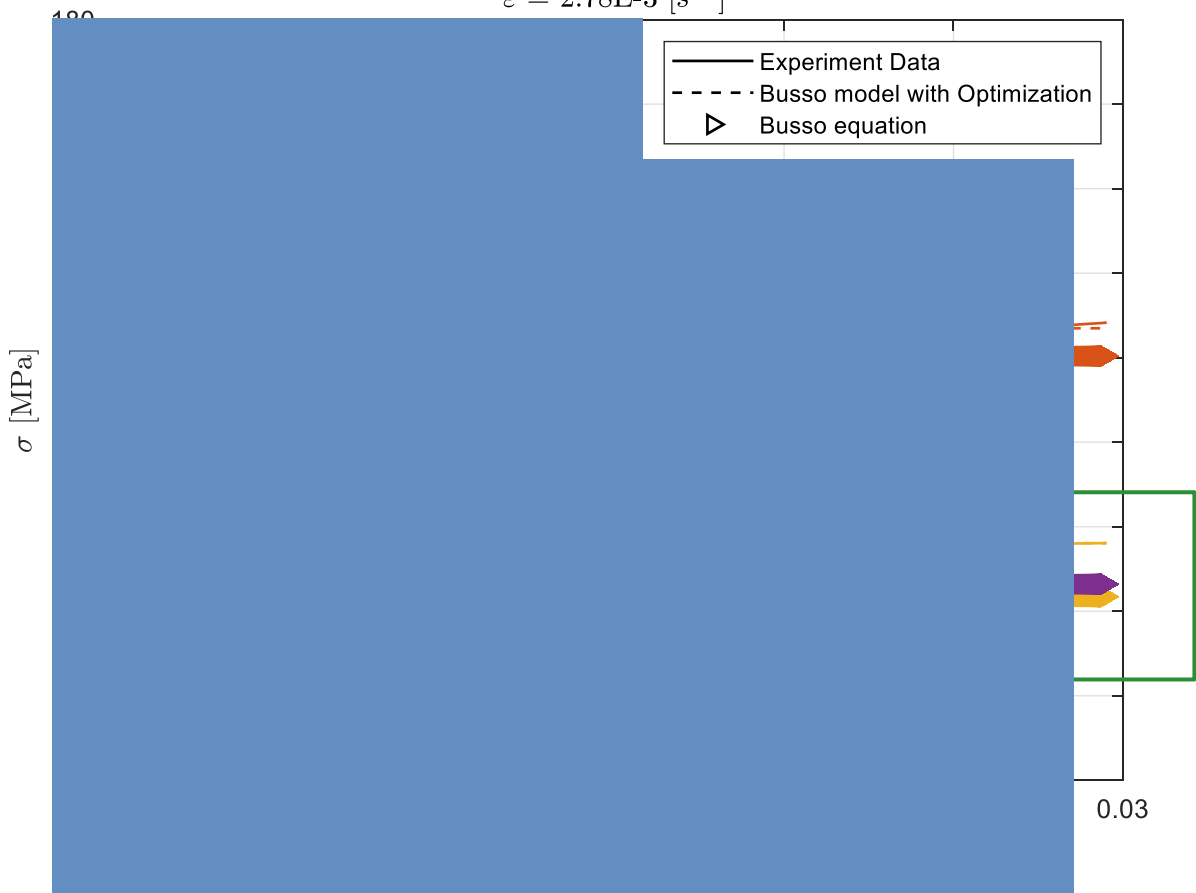
3. Create a temperature-dependent flow equation



Apply exactly the equations generated by Excel

Adjust

Generated σ - ϵ curve
 $\dot{\epsilon} = 2.78\text{E-}3 \text{ [s}^{-1}\text{]}$



Generated σ - ϵ curve
 $\dot{\epsilon} = 2.78\text{E-}3 \text{ [s}^{-1}\text{]}$





3. Create a temperature-dependent flow equation

Final stress-strain curve

Generated σ - ε curve
 $\dot{\varepsilon} = 2.78\text{E-}3 \text{ [s}^{-1}\text{]}$

Final equation

$$\sigma = \sigma_0 A \left\{ 1 - \left[\frac{\theta}{\frac{F_0}{R} \cdot \frac{1}{\ln(\varepsilon_0/\varepsilon_p)}} \right]^{1/q} \right\}^{1/p}$$

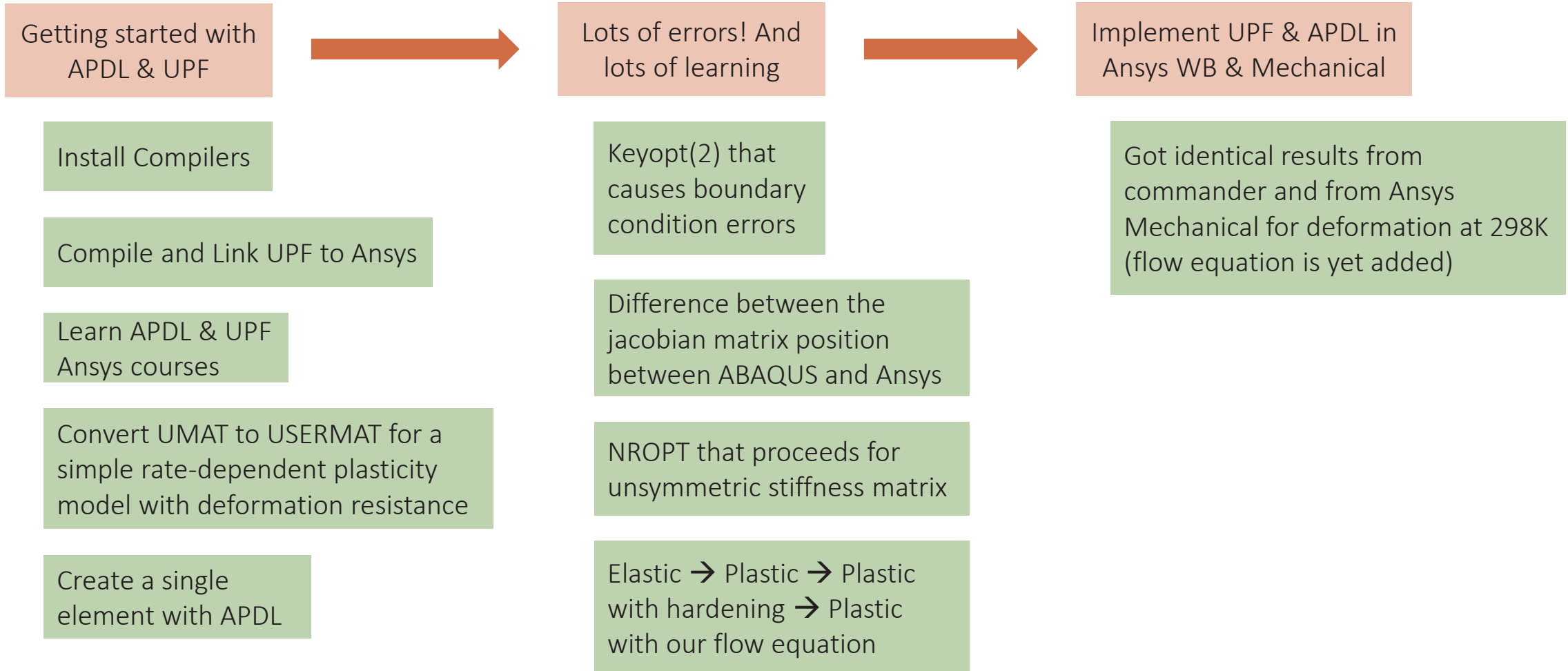
$$\varepsilon_p = \frac{\dot{\varepsilon}_0}{\exp \left\{ \frac{F_0}{\theta \cdot R} \left[1 - \left(\frac{\sigma}{\sigma_0 \cdot A} \right)^p \right]^q \right\}}$$





4. Create an usermat.F file with the developed equation

4.5 Get UPF running in Ansys Mechanical

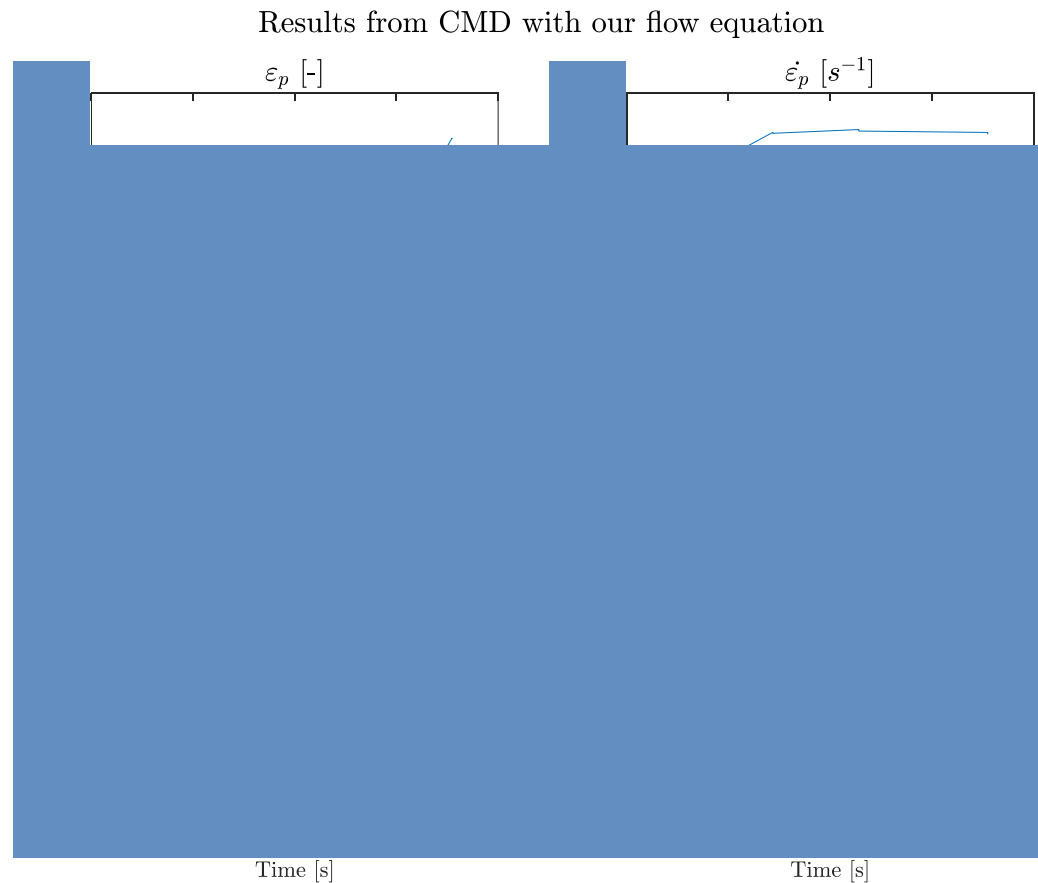




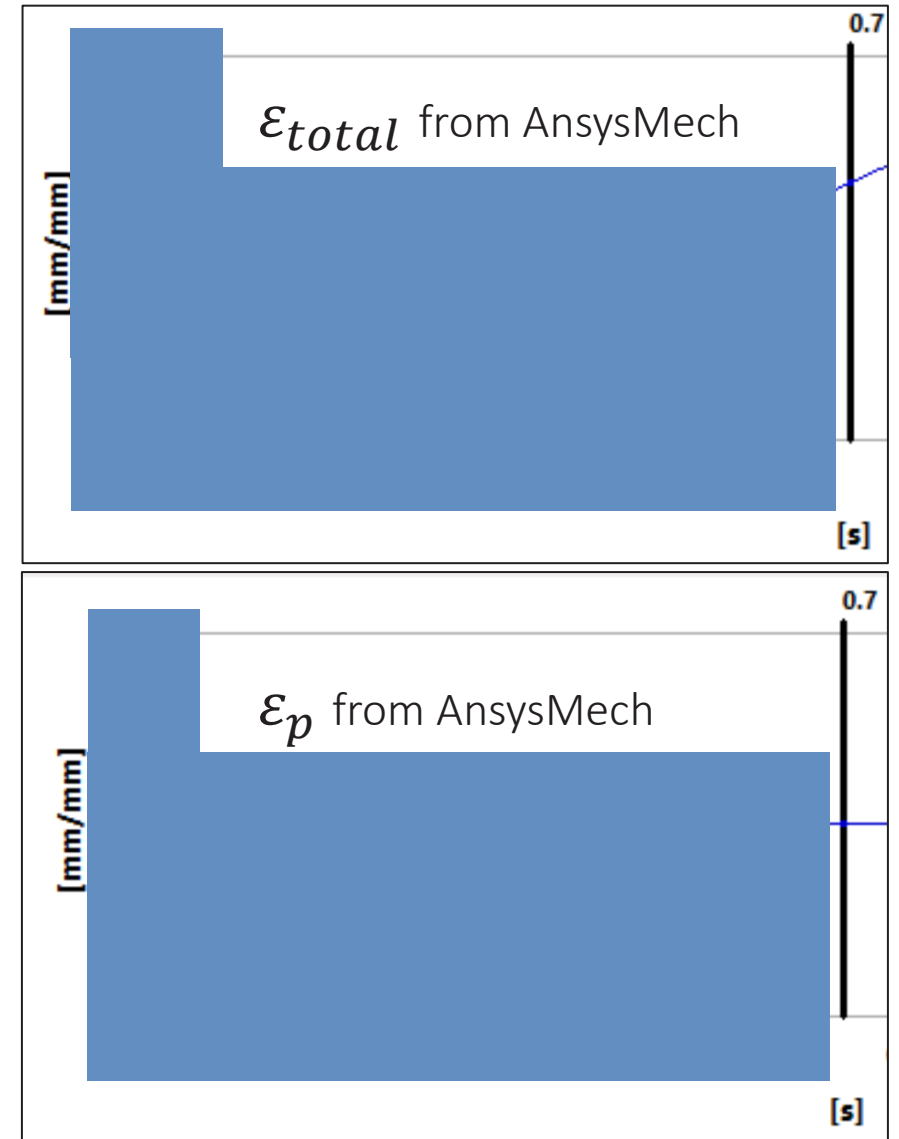
4. Create an usermat.F file with the developed equation

4.5 Get UPF running in Ansys Mechanical

However, results from the Usermat.F with flow equation added show different values from CMD and from Ansys Mechanical
→ Check Mechanical setting



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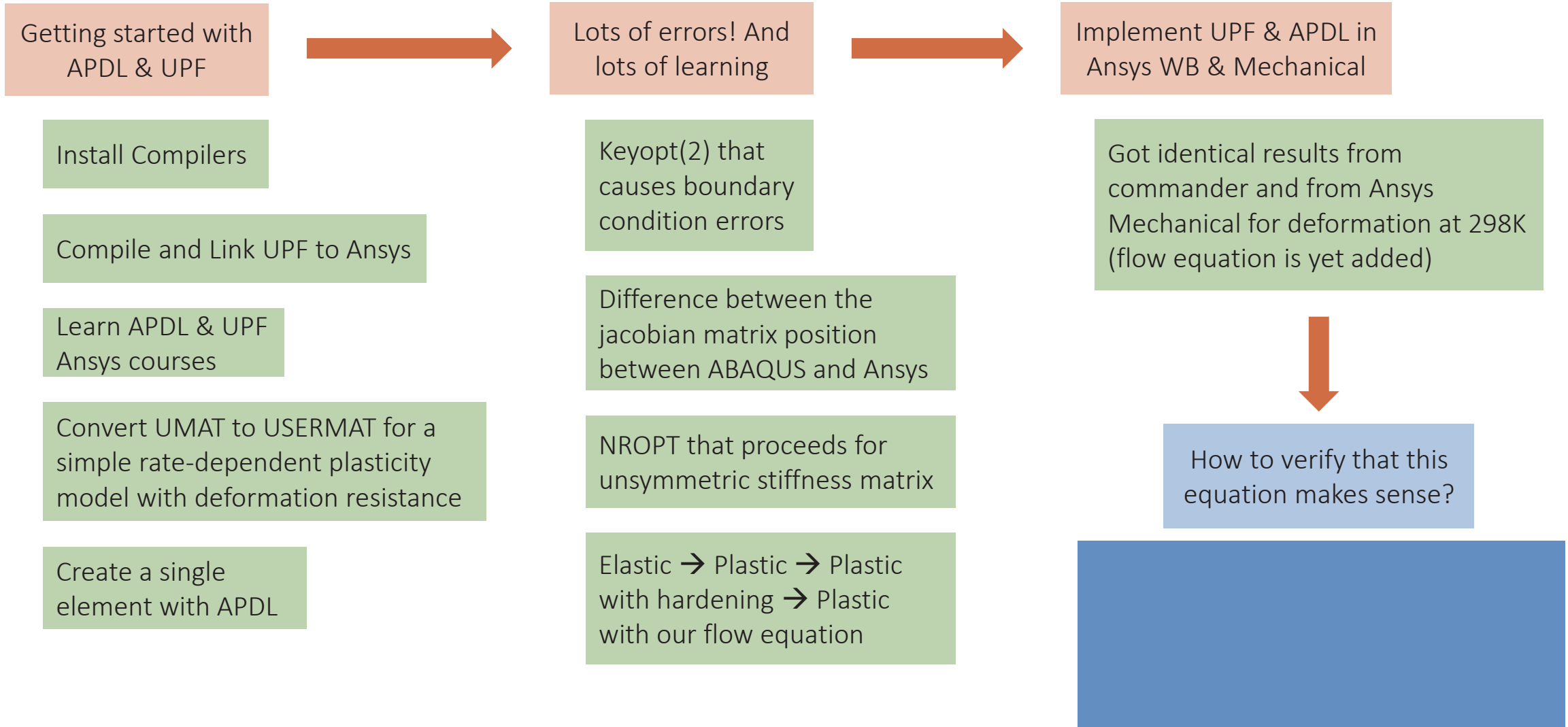
4. Create an usermat.F file with the developed equation
- 4.5 Get UPF running in Ansys Mechanical





4. Create an usermat.F file with the developed equation

4.5 Get UPF running in Ansys Mechanical





Conclusion

- What would I change?
 - Ask more
 - My knowledge and skills scope
- My personal achievements
 - Grateful for the precious learning opportunities (2nd time)
 - Genuinely more interested in FEA
 - Very meaningful to the design of my Master study and career
- Dedication
 - [redacted] – my manager
 - [redacted] – TF team
 - CFS